

# Reasoning and Problem Solving

## Step 5: Compare and Order Less than 1

### National Curriculum Objectives:

Mathematics Year 5: (5F3) [Compare and order fractions whose denominators are all multiples of the same number](#)

### Differentiation:

Questions 1, 4 and 7 (Reasoning)

**Developing** Explain whether a statement is correct when comparing two fractions less than 1 where the denominator is double or half of the starting fraction. Draw a diagram to check.

**Expected** Explain whether a statement is correct when comparing two fractions less than 1 whose denominators are all multiples of the same number or have common numerators. Draw a diagram to check.

**Greater Depth** Explain whether a statement is correct when comparing two fractions less than 1 whose denominators are not direct multiples but have a common factor or have common numerators. Draw a diagram to check.

Questions 2, 5 and 8 (Problem Solving)

**Developing** Use digit cards to complete a more/less than statement comparing fractions less than 1 where the missing denominator is the same, double or half of the starting fractions.

**Expected** Use digit cards to complete a more/less than statement comparing fractions less than 1 where the missing denominators are all multiples of the denominator of the starting fraction.

**Greater Depth** Use digit cards to complete a more/less than statement comparing fractions less than 1 where the missing denominators are not direct multiples but have a common factor with the denominator of the starting fraction.

Questions 3, 6 and 9 (Reasoning)

**Developing** Find the mistake when ordering fractions less than 1 where the denominator is double or half of the starting fraction.

**Expected** Find the mistake when ordering fractions less than 1 whose denominators are all multiples of the same number.

**Greater Depth** Find the mistake when ordering fractions less than 1 whose denominators are not direct multiples but have a common factor.

More [Year 5 and Year 6 Fractions](#) resources.

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## Compare and Order Less than 1

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1a. Wynter is comparing  $\frac{17}{22}$  and  $\frac{9}{11}$ .

I know that is  $\frac{17}{22}$  bigger than  $\frac{9}{11}$  because 17 is bigger than 9.



Is she correct? Show how she could use a diagram to check her answer.



5 R

1b. Xin is comparing the fractions  $\frac{6}{8}$  and  $\frac{1}{4}$ .

I know that  $\frac{6}{8}$  is larger than  $\frac{1}{4}$  because it is equivalent to  $\frac{3}{4}$ .



Is he correct? Show how he could use a diagram to check his answer.



5 R

2a. Use two number cards to complete the equation.

$$\frac{1}{6} < \frac{\boxed{\phantom{00}}}{\boxed{\phantom{00}}} < \frac{3}{6}$$



Find two possibilities.



5 PS

2b. Use two number cards to complete the equation.

$$\frac{2}{9} < \frac{\boxed{\phantom{00}}}{\boxed{\phantom{00}}} < \frac{4}{9}$$



Find two possibilities.



5 PS

3a. Kyle has put these fractions in ascending order.

$$\frac{7}{8}, \frac{5}{8}, \frac{7}{16}, \frac{1}{16}$$

Explain his mistake.

Rewrite the fractions in the correct order as equivalent fractions.



5 R

3b. Holly has put these fractions in ascending order.

$$\frac{1}{5}, \frac{3}{10}, \frac{4}{5}, \frac{7}{10}$$

Explain her mistake.

Rewrite the fractions in the correct order as equivalent fractions.



5 R

## Compare and Order Less than 1

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4a. Luna is comparing the fractions  $\frac{2}{9}$  and  $\frac{2}{3}$ .

I know that  $\frac{2}{9}$  is larger than  $\frac{2}{3}$  because a ninth is three times bigger than a third.



Is she correct? Show how she could use a diagram to check her answer.



5 R

4b. Yussuf is comparing the fractions  $\frac{6}{7}$  and  $\frac{19}{21}$ .

I know that  $\frac{19}{21}$  is larger than  $\frac{6}{7}$  because it is equivalent to  $\frac{18}{21}$ .



Is he correct? Show how he could use a diagram to check his answer.



5 R

5a. Use two number cards to complete the equation.

$$\frac{2}{5} < \frac{\boxed{\phantom{00}}}{\boxed{\phantom{00}}} < \frac{3}{5}$$



Find two possibilities.



5 PS

5b. Use two number cards to complete the equation.

$$\frac{7}{11} < \frac{\boxed{\phantom{00}}}{\boxed{\phantom{00}}} < \frac{8}{11}$$



Find two possibilities.



5 PS

6a. Callum has put these fractions in ascending order.

$$\frac{1}{8}, \frac{3}{4}, \frac{7}{32}, \frac{11}{16}$$

Explain his mistake.

Rewrite the fractions in the correct order as equivalent fractions.



5 R

6b. Julia has put these fractions in descending order.

$$\frac{19}{28}, \frac{3}{14}, \frac{4}{7}, \frac{1}{2}$$

Explain her mistake.

Rewrite the fractions in the correct order as equivalent fractions.



5 R

## Compare and Order Less than 1

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7a. Fran is comparing the fractions  $\frac{8}{25}$  and  $\frac{13}{30}$ .

They are both in the 5 times tables so I can divide by 5 to find equivalent fractions.



Is she correct? Show how she could use a diagram to check her answer.



5 R

7b. Mallory is comparing the fractions  $\frac{7}{18}$  and  $\frac{19}{45}$ .

They are both in the 9 times table so I can use this to find equivalent fractions with a common denominator of 90.



Is he correct? Show how he could use a diagram to check his answer.



5 R

8a. Use two number cards to complete the equation.

$$\frac{8}{45} < \frac{\boxed{\phantom{00}}}{\boxed{\phantom{00}}} < \frac{17}{45}$$



Find two possibilities.



5 PS

8b. Use two number cards to complete the equation.

$$\frac{10}{32} < \frac{\boxed{\phantom{00}}}{\boxed{\phantom{00}}} < \frac{17}{32}$$



Find two possibilities.



5 PS

9a. Mo has put these fractions in ascending order.

$$\frac{7}{20}, \frac{11}{20}, \frac{17}{45}, \frac{83}{90}$$

Explain his mistake.

Rewrite the fractions in the correct order as equivalent fractions.



5 R

9b. Mildred has put these fractions in descending order.

$$\frac{17}{35}, \frac{9}{14}, \frac{1}{7}, \frac{3}{35}$$

Explain her mistake.

Rewrite the fractions in the correct order as equivalent fractions.



5 R

## Reasoning and Problem Solving

### Compare and Order Less than 1

#### Developing

1a. Wynter is not correct. Example answer:

she could use a bar model which shows that  $\frac{9}{11} = \frac{18}{22}$  and  $\frac{18}{22} > \frac{17}{22}$ .

2a.  $\frac{2}{6}$ ,  $\frac{5}{12}$  ( $\frac{2}{5}$  is also a possibility but not expected at this stage).

3a. Kyle has put the fractions in descending order.  $\frac{1}{16}$ ,  $\frac{7}{16}$ ,  $\frac{10}{16}$ ,  $\frac{14}{16}$

#### Expected

4a. Luna is not correct. Example answer: she could use a bar model which shows that  $\frac{2}{3} > \frac{2}{9}$ , as each third is larger than each ninth.

5a.  $\frac{8}{15}$ ,  $\frac{5}{10}$

6a. Callum has ordered the fractions from the numerators.  $\frac{4}{32}$ ,  $\frac{7}{32}$ ,  $\frac{22}{32}$ ,  $\frac{24}{32}$

#### Greater Depth

7a. Fran is not correct. Example answer: she could use a bar model which shows that  $\frac{8}{25}$  and  $\frac{13}{30}$  can not be divided by 5 and produce a whole number as a numerator.

8a.  $\frac{9}{25}$ ,  $\frac{46}{225}$ ,  $\frac{80}{225}$

9a. Mo has ordered the fractions by their denominator but has not found equivalent fractions.  $\frac{63}{180}$ ,  $\frac{68}{180}$ ,  $\frac{99}{180}$ ,  $\frac{166}{180}$

## Reasoning and Problem Solving

### Compare and Order Less than 1

#### Developing

1b. Xin is correct. Example answer: he could use a bar model which shows that  $\frac{6}{8}$  is bigger than  $\frac{2}{8}$ .

2b.  $\frac{3}{9}$ ,  $\frac{7}{18}$

3b. Holly has ordered the fractions by the numerators.  $\frac{2}{10}$ ,  $\frac{3}{10}$ ,  $\frac{7}{10}$ ,  $\frac{8}{10}$

#### Expected

4b. Yussuf is correct. Example answer: he could use a bar model which shows that  $\frac{6}{7} = \frac{18}{21}$  and therefore  $\frac{19}{21} > \frac{18}{21}$ .

5b.  $\frac{15}{22}$ ,  $\frac{22}{33}$

6b. Julia has put the fractions by denominator in descending order.  $\frac{19}{28}$ ,  $\frac{16}{28}$ ,  $\frac{14}{28}$ ,  $\frac{6}{28}$

#### Greater Depth

7b. Mallory is correct. Example answer: he could use a bar model which shows that  $\frac{1}{18} = \frac{5}{90}$  and  $\frac{19}{45} = \frac{38}{90}$ .

8b.  $\frac{8}{24}$ ,  $\frac{31}{96}$ ,  $\frac{37}{96}$

9b. Mildred has ordered the fractions by the numerators.  $\frac{45}{70}$ ,  $\frac{34}{70}$ ,  $\frac{10}{70}$ ,  $\frac{6}{70}$